

# A guide to the aKMC script developed in Henkelman group

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## I. OBTAINING AKMC SCRIPTS

The `akmc` script is part of the `vtstscripts` package written by Henkelman group in the University of Texas at Austin, designed for using Vienna `ab initio` simulation package (VASP). The whole package is written in Perl language and is expected to be working on various platforms. In WINDOWS operation system, ActivePerl program is a possible choice to run the scripts. The whole package can be downloaded via anonymous CVS system (check the guide on <http://theory.cm.utexas.edu/henkelman/code/>). You HAVE TO download the whole `vtstscripts` package in order to run adaptive KMC simulation on VASP, simply because scripts are actually calling each other. By the way, your VASP must be compiled with VTST-TOOLS developed by Henkelman group. The standard VASP package you purchased doesn't work for this aKMC script. The webpage about aKMC is "<http://theory.cm.utexas.edu/vtsttools/akmc/>".

## II. WHAT DOES AKMC SCRIPT DO?

Given a starting system configuration, the `akmc` script handles the whole adaptive KMC simulation using energy and forces calculated from VASP. It first minimizes the configuration it receives, then it will search for saddle points for the minimized configuration and quench each found saddle point into two minima directly connected with it. It can also calculate normal mode frequencies for the initial minimum and its saddles. After finishing saddle point searches, it will calculate the rate constants and prefactors with harmonic transition state theory and get a table of rates for each reaction mechanism. Using that table, it will do a KMC move to select one mechanism and update the system configuration to the end point connected with the minimum energy pathway (or mechanism). The whole process is repeated for the new system configuration. The whole operations are handled by just typing the command "`akmc.pl`".

## III. PREREQUISITE READINGS

Graeme Henkelman and Hannes Jónsson, Long time scale kinetic Monte Carlo simulations without lattice approximation and predefined event table, *J. Chem. Phys.* 115, 9657-9666 (2001) [the original idea of `akmc`]

Lijun Xu and Graeme Henkelman, Adaptive kinetic Monte Carlo for first-principles accelerated dynamics,

*Journal of Chemical Physics* 129, 114104 (2008) [details about algorithms used in this package]

## IV. OPTIONAL READINGS

Graeme Henkelman and Hannes Jónsson, *J. Chem. Phys.* 111, 7010 (1999) [The dimer method]

Lijun Xu, Donghai Mei and Graeme Henkelman, Studying chemical reactions with DFT-based adaptive kinetic Monte Carlo simulations - methanol full decomposition pathways on Cu(100) surface, in preparation [An example of using aKMC to study chemical reactions]

## V. EXAMPLES

After reading this manual, readers are strongly recommended to run the example given on our group webpage (<http://theory.cm.utexas.edu/vtsttools/akmc/>) to see how the scripts and simulations work out.

## VI. GET STARTED

### A. Files used by aKMC script

Create a home directory for aKMC calculations. Put the following files in the aKMC home (or designated) directory, set all the parameters and start the run by typing "`akmc.pl`"

**CONFIG** It has all the control parameters running aKMC simulation. Details will be given in the following section.

**POSCAR** This is the initial configuration given to the program. It will be updated with new structures as simulation goes. The file format must be consistent with VASP POSCAR requirements.

**KPOINTS** Control the k-points setup for VASP calculation.

**POTCAR** Pseudopotential for VASP calculations.

**INCAR\_sp** It instructs how to run a saddle point search in VASP. It is in the same format as VASP INCAR files.

**INCAR\_min** It instructs how to run a geometry minimization in VASP. It is in the same format as VASP INCAR files.

**INCAR\_dynmat** It instructs how to calculate a dynamic matrix in VASP. It is in the same format as VASP INCAR files.

**DISPLACECAR** This is the VASP DISPLACECAR file for dynamic matrix calculation, showing how much each degree of freedom is finitely displaced.

**DISPLACECAR\_sp** This file is in the same format as DISPLACECAR, but each value in the file is the Gaussian width with which a random displacement is to be created for that degree of freedom. It controls how the random saddle point searches are prepared.

**akmc\_submit.pl** This is your own script that submits a job from the directory the job is supposed to run in and prints a job id as the only screen output. It has to be placed in the same folder as akmc.pl and other VTSTSCRIPTS. An example of this scripts is provided on the webpage.

**akmc\_check.pl** This is your own script that takes a job id and checks the status. The only screen output should be "running", or, "stopped", or "queue". It has to be placed in the same folder as akmc.pl and other VTSTSCRIPTS. An example of this scripts is provided on the webpage.

**akmc\_kill.pl** This is your own script that kills a job. It has to be placed in the same folder as akmc.pl and other VTSTSCRIPTS. An example of this scripts is provided on the webpage.

**akmc\_sp.sub** This is the submission script used by akmc\_submit.pl for submitting saddle point searching jobs to the queue system.

**akmc\_min.sub** This is the submission script used by akmc\_submit.pl for minimization jobs to the queue system.

**akmc\_dynmat.sub** This is the submission script used by akmc\_submit.pl for dynamic matrix calculation jobs to the queue system.

## B. Files and folders created by aKMC script

After running aKMC, there will be new files and folders to be created automatically. In the following list, you will see them in the order of being created by the script.

**jobs.dat** This file contains all the job information: work directory, job id, job type, energy, force, curvature.

**min** This folder is created to run the very beginning minimization. The minimized structure will be used to start the search of saddle points. A minimized structure represents a state of the system.

**akmc.dat** This file keeps the information of each aKMC step: showing the configuration of the step, barrier, accumulated time, etc. It is also a key file for the script to figure out the stop point from the previous running of "akmc.pl".

**st0001** After the initial minimization, this state folder is created to contain all the saddle point searching processes for the first state. There are subfolders and files inside this directory. We take the first one st0001 as the example to show the tree structure of the state folders.

**st0001/POSCAR, etc.** This is the POSCAR copied from the AKMC home directory as the configuration of the state "st0001". Other types of files in home directory such as POTCAR, INCAR\_min, INCAR\_sp, DISPLACECAR\_sp and KPOINTS will also be copied into this state folder.

**st0001/neighborlist.dat** This neighbor list file, if created, is for random displacement. Details are in the reference.

**st0001/st.dat** This file is the key file for a state: it records how many saddle point searches are running in the sr0001, and the evaluation of each saddle searching process: good, bad or something else. Together with jobs.dat, it does the main control of the aKMC job running. Any manual handle should target towards "jobs.dat" and "st.dat".

**st0001/pr0001** This folder is the first saddle point search for state "st0001". It has subfolders and files.

**st0001/pr0002** This folder is the second saddle point search for state "st0001". It has subfolders and files.

**st0001/pr0001/POSCAR** POSCAR for a saddle point searching job in VASP. It is created by randomly displacing the state POSCAR.

**st0001/pr0001/INCAR** INCAR for a saddle point searching job in VASP. Note: all three INCAR\_\* files are copied inside folder st0001 and pr0001. INCAR\_sp will be copied into INCAR automatically when the job is being submitted. akmc\_sp.sub will be copied into akmc.sub which is the standard submission file in the akmc\_submit.pl script.

**st0001/pr0001/POTCAR** Same POTCAR file as in the home directory.

**st0001/pr0001/KPOINTS** Same KPOINTS file as in the home directory.

**st0001/pr0001/inter** A unfinished but stopped job are cleaned up into this inter, it will be renamed to inter1, inter2, as more come in, but this "inter" is the most recent one. It is same as what vfin.pl does in our normal VASP job cleanup.

**st0001/pr0001/final** A converged (saddle searching) job is cleaned up into this folder. It is same as what vfin.pl does in our normal VASP job cleanup. DO NOT rename this folder. Both “inter” and “final” are required standard folder names in this package.

**st0001/pr0001/POSCAR\_sp** It is the saddle point configuration file. The CONTCAR (or CENTCAR) of a converged job will be copied into this file. DO NOT rename this file.

**st0001/pr0001/dynmat** If dynamic matrix calculation is required, this folder will be created to do the dynmat calculation. POSCAR\_sp will be copied into dynmat/POSCAR, INCAR\_dynmat will be copied into dynmat/INCAR, etc.

**st0001/pr0001/dynmat/final** A converged dynmat job is cleaned up into this folder. It is same as what vfin.pl does in our normal VASP job cleanup.

**st0001/pr0001/mins** This folder contains jobs of quenching the converged saddle into two adjacent minima.

**st0001/pr0001/mins/min1** This folder contains the minimization of one image along the MEP. A normal VASP minimization job.

**st0001/pr0001/mins/min2** This folder contains the minimization of the other image along the MEP. A normal VASP minimization job.

**st0001/pr0001/mins/min1/final** A folder for converged minimization job. Same as before.

**st0001/pr0001/mins/min2/final** A folder for converged minimization job. Same as before.

**st0001/jobs.dat** Once st0001 is done, the jobs.dat in the aKMC home directory will be copied into the state folder st0001.

**st0002** If st0001 is finished, KMC will make a move and update the system into a new state. Then st0002 will be created to start the saddle point searches for the new state. AaKMC continues like this until it reaches the maximum number of steps indicated in **CONFIG** file.

**StEnergyFile** This is to store the energy of each state the AKMC simulation has visited. It is for the sake of avoiding reading the st.dat when the code goes back to check if the new state has appeared somewhere before. Any state in this file must be a finished state.

## VII. FOUR KEY FILES: CONFIG, ST.DAT, JOBS.DAT AND AKMC.DAT

Those four files determine the main stream of the aKMC script.

## A. CONFIG

Here is an sample “CONFIG” file.

---

```

MaxJobs = 12
RandSeed = 5
NumSearches = 10
AkmcSteps = 100000
SimR = 0.1
NumKT = 20
Temperature = 300.0
Ediffmax = 0.05
Rdiffmax = 0.04
SearchesAlgo = dimer
BarrierMAX = 10.0
JobFile = jobs.dat
StFile = st.dat
AkmcFile = akmc.dat
DynMatFile = freq.dat
Prefactor = 1.0e12
RateTableFile = RateTableFile.dat
OldRunDirFile = OldRunDirFile.dat
StEnergyFile = StEnergyFile.dat
GrabQuenched = 1
Population = 0.2
PrRecycleAll = 1
PrRecycle = 1
PrRecycleShift = 1
SurfaceRecShift = 1
ConvergenceAlgo = 1
equivalency = 1
DisplaceAlgo = 1
DisplaceRange = 3
NN_rcut = 2.6
MaxCoordNum = 8
UseKDB = 0

```

---

File “config” is in the aKMC home directory and contains the following flags.

**MaxJobs** The maximum number of jobs can be submitted through aKMC. This number must be smaller than the maximum allowed by the queue system. For example, if the queue allows you to have at most 8 jobs running and waiting in the queue and you use three jobs to do things other than AKMC, you will have to set MaxJobs to 8-3=5. You have to tell the scripts how many jobs are allowed. There is no way for the script to figure out the number by itself.

**NumSearches** The number of searches for convergence standard. If there are no new good saddle points found during that many straight successful searches, the searching will stop and an event table will be compiled for KMC. Default: 10. Details are in the reference.

**AkmcSteps** The total number of KMC steps. Use “1” for mechanism study. Default: 1

**SimR** The distance (in Å) between two images centered around the saddle point along the minimum energy path. Those two images are expected to roll into two end points of the MEP upon minimization. Default: 0.1

**Temperature** The temperature in kelvin. Default: 77

**NumKT** The energy gap above the lowest saddle point. Saddle points above the highest point are considered unimportant to the final rate table. The unit is kT and T is for temperature. Normally, this number is at least 10, which means 10 times thermal energy at the temperature. Default: 20

**EdiffMax** The maximum energy difference (in eV) between two configurations, below which geometry difference will be calculated. Default: 0.05

**RdiffMax** The maximum difference (in Å) between any two corresponding atoms from two configurations, below which two geometries will be considered as identical. In aKMC, two POSCAR files are frequently compared to determine if they are for the same geometry. Default: 0.05

**SearchAlgo** The saddle point searching mechanisms. Right now, it can only be “dimer”. “Lanzcos” may be added to the script in the future. Default: “dimer”.

**BarrierMax** The maximum energy allowed before killing a search for the searching point energy being too high. Default: 10

**JobFile** The filename for jobs.dat in the aKMC home directory. Default: “jobs.dat”.

**StFile** The file name for st.dat in the state folder (such as st0001). Default: “st.dat”

**AkmcFile** The file name for akmc.dat. Default: “akmc.dat”

**DynMatFile** The file containing normal mode frequencies. Keep the default name unless you modify the dymatrix.pl script. Default: “freq.dat”.

**Prefactor** The dynamic matrix calculation will be disabled if this flag is turned on. The positive value will be used for every process in the coming calculations. You have to keep this flag consistent throughout your whole aKMC calculations. Default: 0 (disabled)

**RateTableFile** The file for storing the rate table. Default: “RateTableFile.dat”

**OldRunDirFile** The file listing all the database folders. Default: “OldRunDirFile”

**StEnergyFile** The energy of each state’s configuration is listed in here. Default: “StEnergyFile”.

**Population** An obsolete convergence standard. It will be only used for ConvergenceAlgo=2 which we don’t recommend. Default: 0

**GrabQuenched** If it is set to be 1, the code will check if the newly converged saddle has been quenched before (not limited to this state, including all the previous states and database). Default: 0

**PrRecycleAll** If it is set to be 1, the code will check if the new state is one of the end points in those mechanisms have been found in previous states and database. If yes, the code copies those processes and recover those saddles for the new state. Default: 1.

**PrRecycle** If it is set to be 1, any good saddle from the previous (or equivalent) state will be recycled and reconverged for the new state. Default: 0.

**PrRecycleShift** If it is set to be 1, a vector-shifting recycle will be used. Default: 0.

**SurfaceRecShift** If it is set to be 1, the system will be a surface science problem: adsorbates on substrate. In POSCAR, adsorbates will be listed as the last group. Any good saddle from the previous state will be reconverged by adjusting the adsorbate orientation. This is not a mature technique. We do not recommend it unless you are familiar with the code itself. Default: 0.

**ConvergenceAlgo** The key flag controlling the ending of the saddle point searches: “0” for a fixed number of saddle searches; “1” for a dynamic standard (coupled with “NumKT” flag)

**Equivalency** If it is set to be 1, the system will test if the new state configuration is actually equivalent to some previous states by checking the one-to-one matching between atoms in two POSCAR files (or “the radial distribution function” of adsorbates if “SurfaceRecShift” is set to 1.). Saddle points from any equivalent state will be reshuffled based on the matching and used directly. Default: 0.

**Screenoutput** the file for keeping the screen output from running “akmc.pl”. Default: “out.dat”.

**DisplaceAlgo** The displacing algorithm used in creating random dimer configurations: “0” for selecting one of the most under-coordinated atoms as the displacement center; “1” for one of the choosing the less ( $j = \text{MaxCoordNum}$ ) coordinated atoms as the displacement center; “2” for dividing the surface into islands and doing the “0” option in islands; “3” for dividing the surface atoms into islands and doing the “1” option in islands; any other values will lead to a random atom to be selected as the displacement center. Note: only those atoms (or degrees of freedom) marked as non-zero in the DISPLACECAR.sp can be the candidate displacement center in any of those algorithms. Default: 1. Details are in the reference. It is important to be familiar with these algorithms.

**DisplaceRange** The radius around the displacement center within which all of those atoms will be displaced by a random vector. Default: 3.

**NN\_rcut** The maximum pair distance for two nearest neighbors. Default: 2.6

**MaxCoordNum** The maximum coordination number used in DisplaceAlgo=1. Default: 8.

**BoltzmanEqu** The threshold for two states being in Boltzman equilibrium: if one MEP shared by two states are dominating at least that amount of percentage in each rate table. Default: 0.999999.

**UseKDB** This is about using database to prepare saddle point searches for the new state. If it is on, random searches will be done after using the initial guesses from databases. Default: 0

**KDBcutoff** This is a standard used in UseKDB to determine how similar two systems should be in order to exchange saddle point information with each other. Default: 0.1

## B. ST.DAT

Here is an sample ‘st.dat’ file.

---

```
st0001 -376.931759
status running
dynmat done
NumSearchesLeft 10
numprst 12
process status quality barrier final/(min1) final/(min2)
pr0001 done good 1.997 mins/min1 -375.549
pr0002 done good 0.595 mins/min1 -376.521
pr0003 done good 2.463 mins/min1 -375.566
pr0004 done bad 1.809 -375.988 -375.339
pr0005 killed saddleenergytoohigh_search na na na
pr0006 done bad 3.126 -375.409 -376.264
pr0007 killed positive_curvature_search na na na
pr0008 done bad 0.795 -376.433 -376.931
pr0009 done repeat*pr0008 0.795 na na
pr0010 done repeat*pr0002 0.595 na na
pr0011 quench promising 2.531 na na
pr0012 search pending na na na
```

---

File “st.dat” is in the state folder (such as st0001) and contains the following information (Let’s take st0001/st.dat as the example).

**First line** “st0001 -376.931759” for the relative address and energy of the state.

**Second line** “status running” for indicating the state is not done yet. “status done” is for a done state.

**Third line** “dynmat running” for indicating the dynamic matrix calculation for the state configuration has not finished yet. “dynmat done” means it is either finished or tuned off by setting the Prefactor flag in CONFIG file.

**Fourth line** “NumSearchesLeft 10” shows how many more good saddle searches without seeing a new saddle are left. The state will be taken as “done” if it is set to zero.

**Fifth line** “numprst 12” shows that there are 12 process folders for 12 saddle point searching jobs.

**Sixth line** It is an optional description line showing the meaning of each column in the following parts of the file: “process status quality barrier final/(min1(ev)) final/min2(ev)”

**Next line: column one** It is the folder name for the process: e.g., pr0001, pr0002. etc.

**Next line: column two** It is the status for the process: “done” means the searching (and dynmat if needed) and quenching are all finished. Otherwise, the status would be “search”, or “quench”, or “dynmat” for each type of operations. If the search is killed for some reason, “killed” will appear in this column and a reason follows it.

**Next line: column three** It is the quality of the saddle point: “good” means one and only one of the end points of the minimum energy path is “same” as the configuration of the state (i.e., same as the POSCAR in folder st000x); “bad” means neither of the end points is same as the state configuration; “promising” means the barrier of the saddle (relative to the initial state) is not larger than “BarrierMax” in CONFIG file and the saddle is being quenched to determine if it is good or not; “bad” can also mean other situations including negative barrier, barrier being too high, etc; “repeat\*pr0003” means this saddle is same as the saddle point in pr0003 and pr0003 has been finished (or at least the quenching jobs have been finished); “pending” means the saddle is not converged yet.

**Next line: column four** It is the barrier of the saddle point in eV.

**Next line: column five** If the saddle is “good”, this column will record the address of the final state of the minimum energy path (the initial state will be same as the state configuration), e.g., “mins/min1” means that the final state is in “st0001/pr0001/mins/min1/POSCAR” and implies that the initial state is “st0001/pr0001/mins/min2/POSCAR” which is same as “st0001/POSCAR”. If the saddle is “bad”, this column will be simply the energy of the state in “st0001/mins/min1/” in eV. Otherwise, an “na” will be put in there for “not available”.

**Next line: column six** If the saddle is “good”, this column will record energy of the state in column 5. If the saddle is “bad”, this column will be simply the energy of the state in “st0001/mins/min2/” in eV. Otherwise, an “na” will be put in there for “not available”.

### C. JOBS.DAT

Here is an sample “jobs.dat” file.

---

```
location Status JobId JobType Energy Force Curv.
st0008/pr0001 completed 1 dimer -374.9 0.01 -1.34
st0008/pr0001/mins/min1 queue 2 minimization - - -
st0008/pr0001/mins/min1 queue 3 minimization - - -
```

---

File “jobs.dat” is in the aKMC home directory and contains the following information.

**First line** It is a mandatory description line showing the meaning of each column in the following parts of the file. “joblocation JobStatus JobId JobType Energy(eV) Force(eV/A) Curvature” are quite self-explanatory.

**column one** This is the relative address of the job location.

**column two** This is the job status: “submitted”, “queue”, “running”, “stopped”, “completed” or “2bsubmitted”. Among them, “completed” means the job has really converged based on the INCAR settings. “2bsubmitted” means somehow the job was not successfully submitted and the script will try next time; the reasons include the number of jobs in the queue is exceeding the MaxJobs in CONFIG or the queue system limit, or just bad files.

**column three** This is the job type which can be “dimer”, “minimization”, or “dynmat”.

**column four to six** Those are for energy, force and curvature, respectively. No values will be marked “na”.

It is mandatory that each process in the state must have an entry in the jobs file. If the users want to add some processes in the state folder (e.g., st0001), they also need to create entries in jobs.dat for those added processes. If a trivial jobid is needed so that the script will take the new processes as “finished saddle point searches”, we recommend using “jobid\_marker”.

### D. AKMC.DAT

Here is an sample ‘akmc.dat’ file.

---

```
Step stnumber property address stenergy(eV) ften-
ergy(eV) ChosenPr steptime(s) totaltime(s)
1 st0001 new st0001 -374.2 -374.8 pr0002 3.7758e-07
3.7758e-07
2 st0002 new st0002 -374.8 -375.4 pr0008 1.6978e-07
5.4736e-07
3 st0003 new st0003 -375.4 -375.5 pr0012 1.0949e-07
6.5685e-07
4 st0004 new st0004 -375.5 -376.0 pr0020 1.1486e-05
1.214285e-05
```

```
5 st0005 new st0005 -376.0 -375.7 pr0032 2.4170e-05
3.631285e-05
6 st0003 repeat st0003 -375.7 -376.0 pr0011 2.4171e-05
6.048385e-05
7 st0006 new st0006 -375.7 -376.0 pr0018 2.4171e-05
8.465485e-05
8 st0007 repeat /somewhere/st0002 -375.7 -376.0
pr0038 2.4171e-05 1.0882585e-04
9 st0008 new st0008 -375.7 -376.0 pr0029 1.6978e-07
1.0899563e-04
```

---

File “akmc.dat” is in the aKMC home directory and contains the following information.

**First line** It is an mandatory description line showing the meaning of each column in the following parts of the file: “akmcStep stnumber property target stenergy(eV) ftenenergy(eV) totaltime(s)”.

**column one** This tells the simulation is at which KMC step.

**column two** This is the name of the state.

**column third** This tells if the state at that time was new or not. “new” means that state had never appeared before (including in the possible database) while “repeat” means the opposite.

**column four** This is the address of the state. It looks trivial at most time, but if the state is repeated in some database, this address will be the key to get access to the information of the repeated state (see st0007 in the sample file).

**column five** The chosen process from that state.

**column six** The energy of the state, in eV.

**column seven** The energy of the chosen state, in eV.

**column eight** The time elapse from this state, in eV

**column nine** The total simulation time, in seconds.

### VIII. WHAT HAPPENS WHEN YOU TYPE “AKMC.PL”

First of all, you should only run akmc.pl in the aKMC home directory, i.e., where the “config” file is. After you type the command of “akmc.pl”, the script first reads “config” file. Then it checks MaxJobs set by the “config” file. It has to be a non-negative number. After that, the script decides if the dynamic matrix calculation is necessary. The next step is to figure out the status of this aKMC run. It reads the “akmc.dat” file to pick up its memory of the previous step and current step and figure out if the current is a new state, or if it has been started, etc. If the script finds the current step (state) is still being calculated, it will tell the code (“akmc.check.pl)

to check jobs.dat file and update the job status information. Then it will switch to the main loop by reading information from “st.dat” file in the current state folder and handles each process based on its status and the updated job information. The screen output will tell you the progress of the script running.

## IX. INTRODUCTION TO ADAPTIVE KINETIC MONTE CARLO SIMULATION

The original idea about adaptive kinetic Monte Carlo (aKMC) simulation was presented in the article by Graeme Henkelman and Hannes Jónsson [*G. Henkelman and H. Jónsson, Long time scale kinetic Monte Carlo simulations without lattice approximation and predefined event table, J. Chem. Phys. 115, 9657-9666 (2001)*]. A new article on the improvement of aKMC is published by Lijun Xu and Graeme Henkelman [*Lijun Xu and Graeme Henkelman, Adaptive kinetic Monte Carlo for first-principles accelerated dynamics, Journal of Chemical Physics 129, 114104 (2008)*]. The following paragraphs have also been posted on the web page of Henkelman group in the University of Texas at Austin (<http://theory.cm.utexas.edu/henkelman/research/ltd/>).

### A. Limits of Molecular Dynamics

Long time dynamics (LTD) refers to dynamic simulation of physical and chemical processes over the time scale much longer than traditional molecular dynamics does. Molecular dynamics simulates dynamic processes by solving Newtonian equation of motion via finite difference approximation. The time step is typically at the femto-second level. Therefore, molecular dynamics can only simulate events efficiently up to pico- or nano-seconds. However, a lot of interesting events, such as diffusions and chemical reactions, can only happen at the time scale of milli-seconds, seconds or even hours or days. Those events are usually called “infrequent”, “rare”, or “slow” events. Obviously, it would take an enormous number of steps to simulate rare events with molecular dynamics.

### B. Transition State Theory

The potential energy surface (PES) is a multi-dimensional surface on which each energy point corresponds to a possible configuration of the system. There are regions where the system spends most of its time. Those regions are usually local minima or low energy areas corresponding to stable system configurations (e.g., a stable particle, a favorable adsorbate conformation etc). Meanwhile, there are also regions the system rarely visits. From the view of dynamics on the PES, system always vibrates around those local minima (or basin areas), while

it occasionally hops from one local minimum to another. That hopping could contribute most to the LTD process.

Transition state theory (TST) assumes that system has to cross over some transition state (usually a narrow bottle-neck type of high energy region on the PES) which the system rarely visits, to move from one local minimum to another. TST uses a statistical estimation of how fast the transition is in terms of a rate constant at a certain temperature. For a lot of solid systems, a harmonic approximation (hTST) can be assumed for both minima and transition states. Then, TST can give a most probable transition pathway (minimum energy path or mechanism) which connects two local minima via a saddle point. The rate of the transition can be calculated from the energies and normal modes of both local minimum and saddle point. Therefore, TST provides a solution to simulate the most important part of LTD - rare events. Combined with molecular dynamics simulation of frequent events, a multiple time scale of LTD can be achieved with good efficiency.

### C. Kinetic Monte Carlo

Combined with hTST, kinetic Monte Carlo (KMC) simulation is very useful in long time scale dynamics. Given those rate constants calculated from transition state theory, KMC can build an event table with all the transition mechanisms (for rare events). An event can be selected from Boltzman distribution by generating a random number; fast events have larger rate constants and therefore, are more probable to be chosen. The system configuration will be updated the end point of the chosen minimum energy pathway. The whole process is repeated for the new state. By this means, the evolution of the system on the PES can be efficiently simulated over a long time scale.

### D. Adaptive kinetic Monte Carlo

The key step in KMC combined with hTST is to build a reliable event table for each state the system visits. It is rare that those events in the table can be known beforehand (except for some simple systems). In most cases, the event table has to be built on the fly (or adaptively) for each specific state. We call this type of long time scale simulation “adaptive kinetic Monte Carlo” (aKMC). It is going to be our main LTD tool.

### E. Saddle point searching methods

By now, the whole LTD problem has been reduced to finding those saddle points for a given configuration. There are quite a few methods on searching for saddle points (see review). Our choice is the Dimer Method developed by Graeme Henkelman and Hannes Jansson.

It's a minimum mode following method using only the first order derivative of the potential.

#### **F. Empirical potential and DFT**

Adaptive kinetic Monte Carlo simulation based on dimer method requires an accurate evaluation of the system energy and forces on atoms. Based on how energy and forces are calculated, aKMC can be carried out through either empirical potentials or first principle methods such as density functional theory. Our group has developed a distributed computing system (EON) for using empirical potentials in the aKMC simulation.

It takes advantage of idle computing resources on the internet. The server sends out dimer searching jobs to client computers, collects the results when the jobs are finished and does the KMC steps. If there are no reliable empirical potentials available for the system, some quantum calculations have to be used to get energy and forces for the system. We have also developed a scripting program (AKMC) to do the aKMC simulation through the VASP density functional calculations. The AKMC scripts handles every detail of the adaptive kinetic Monte Carlo simulation and frees people from tedious things such as submitting and checking jobs. A single step of aKMC simulation can be a powerful tool for mechanism studies in Surface Science and Catalysis.